A Text-Mining Approach to the Authorship Attribution Problem of *Dream of the Red Chamber*

Hsieh-Chang Tu* and Jieh Hsiang**
National Taiwan University

Abstract

*Dream of the Red Chamber* (DRC), written in the 18th century, is among the greatest Chinese classic novels. Indeed, so many studies have been devoted to this work that the term *Redology* was created to designate this field of research. (The 2,200-page book by Pan 1974 described earlier works in Redology.) DRC has 120 chapters. In 1921, Hu Shi (胡適) provided solid evidence to show that the first 80 chapters were written by Cao Xueqin (曹雪芹) based on his life. He also attributed the remaining 40 chapters to Gao E (高鶚) (Hu 1921). While the first conclusion is commonly accepted, the second is still not settled.

Researchers have also used statistical methods to study this problem. They usually use certain pre-defined linguistic features, usually a set of function words, to check whether the feature frequencies in the first 80 chapters are significantly different from the last 40. Interestingly, however, people came to different conclusions when different features were chosen.

In this paper we propose a text-mining approach to the DRC author attribution problem. We define a mining function to find terms that clearly show discrepancies between the two corpuses. Some of the terms are semantic in nature, thus avoiding the pitfalls with the more syntactic function words approach. In addition to supporting the claim that the first 80 chapters and the last 40 were written by different authors, a somewhat surprising side result is the evidences that show Chapters 64 and 67, two chapters missing from the oldest existing edition, could also have been written by someone other than Cao Xueqin.

1. Introduction

Authorship attribution is a well-researched subject. Brinegar (1963) used word

---

* tu@turing.csie.ntu.edu.tw
** jhsiang@ntu.edu.tw
length as the text feature to conclude that the 10 Quintus Curtius Snodgrass letters were not written by Mark Twain. Thisted and Efron (1986) adopted a model from ecological studies to infer that a newly-discovered nine-stanza poem was written by William Shakespeare. Recent approaches, that usually assume that the contexts being compared are different, make use of most frequent words and clustering analysis to identify the most likely author (Peng and Hengartner 2001, Burrows 2002, Hoover 2004, Malyutov 2006, Stamatatos 2009, Jockers and Witten 2010).

A well-known author attribution problem in Chinese literature is the author of the last 40 chapters of the novel *Dream of the Red Chamber*. Past stylistic studies lead to contradictory conclusions due to different feature selections and experiment designs. Karlgren (1952), Chan (1986), and He (2002) concluded that the entire DRC was written by the same person, while Zhao and Chen (1975), Yu (1998), and Yang (2003) showed significant differences between the first 80 and the last 40 chapters.

Most of these work began from choosing certain linguistic features (usually *function words*). A hypothesis testing method is then deployed to check whether the frequency distributions of features in the first 80 chapters are significantly different from those in the last 40. Yang (2003) used a different approach. They first partitioned DRC into 12 documents, each with 10 chapters. Instead of using pre-defined words, they designed a simple function that used the frequencies of unigrams to associate similarities of each pair of the 12 documents. They found strong similarities in the first 2 documents (containing Chapters 1-20), the next 6 documents (Chapters 21-80), and the final 4 (Chapters 81-120), and thus concluded that the final 40 chapters were written by a different author. However, using the same reasoning, one could also conclude that the first 20 chapters and the middle 60 were written by different authors.

2. **Our text-mining approach**

We propose a text-mining approach to the DRC author attribution problem. Instead of choosing a pre-defined set of words, we design a mining function to generate candidate words. In addition to term frequencies, we also consider another important factor: the number of chapters in which a term appears.

2.1 **The edition question**

The first question is to choose a proper edition. DRC has scores of editions, the earliest of which (dated 1754) contains merely 16 chapters, and the second, *gengchen*.
The earliest existing version with 120 chapters appeared in 1791, edited by Cheng Weiyuan and Gao E. The full text we chose was the one provided by YuanZe University, which is the closest to the earliest editions. As a side note, since the gengchen edition has only 78 chapters, we need to decide whether Chapters 64 and 67 should be included in our study. We finally decided to leave them in. Our analysis actually leads to the conclusion that these two chapters were written by someone else.

2.2 The text-mining function

Regarding each chapter as one document, we use $A$ and $B$ to denote the corpuses of the first 80 chapters and the last 40 respectively. Thus $|A| = 80$ and $|B| = 40$. We use $t \in d$ to mean that the term $t$ occurs in document $d$. Let $D_t = \{d: t \in d, d \in D\}$ be the subset of $D$ which contains term $t$. We call $|D_t|$ the document frequency of $t$ in $D$. Given a term $t$ and a document set $D$, we define the average document frequency of $t$ in $D$ to be $p_t(D) = |D_t|/|D|$. Intuitively, it means that on the average any document in $D$ has probability $p_t(D)$ to contain the term $t$.

We define the text-mining function as follow:

$$f(t) = \frac{\max(p_t(A), p_t(B)) + k}{\min(p_t(A), p_t(B)) + k},$$

where a constant $k$ is added to avoid the case $f(t) = \infty$ when $p_t(A)$ or $p_t(B)$ equals 0. We set $k$ to be 0.02 in our experiments. To better understand how this function works, consider the case that $p_t(A) \geq p_t(B)$ and $k=0$. Then $f(t) = p_t(A)/p_t(B)$ and a bigger $f(t)$ has the higher ratio of $p_t(A)$ to $p_t(B)$. Thus a high-scored $f(t)$ means that the average document frequency of term $t$ in $A$ is significantly different from that in $B$.

The top 5 unigrams and top 10 bigrams obtained through $f(t)$ are given in Table 1. We remark that we studied the top 30 unigrams and bigrams, and they all showed

| $t$ | $f(t)$ | $|A_t|$ | $|B_t|$ |
|-----|--------|--------|--------|
| 1 嬤 | 22.3   | 34     | 0      |
| 2 裂 | 22.3   | 34     | 0      |
| 3 嗎 | 22.2   | 1      | 28     |
| 4 展 | 17.3   | 26     | 0      |
| 5 疆 | 14.8   | 0      | 11     |

Table 1. The top 5 high-scored unigrams and top 10 bigrams computed by the mining function $f(t)$. 

edition (庚辰本) of 1760, has 78 chapters (Chapters 1-80 except 64 and 67). The earliest existing version with 120 chapters appeared in 1791, edited by Cheng Weiyuan and Gao E. The full text we chose was the one provided by YuanZe University, which is the closest to the earliest editions. As a side note, since the gengchen edition has only 78 chapters, we need to decide whether Chapters 64 and 67 should be included in our study. We finally decided to leave them in. Our analysis actually leads to the conclusion that these two chapters were written by someone else.

2.2 The text-mining function

Regarding each chapter as one document, we use $A$ and $B$ to denote the corpuses of the first 80 chapters and the last 40 respectively. Thus $|A| = 80$ and $|B| = 40$. We use $t \in d$ to mean that the term $t$ occurs in document $d$. Let $D_t = \{d: t \in d, d \in D\}$ be the subset of $D$ which contains term $t$. We call $|D_t|$ the document frequency of $t$ in $D$. Given a term $t$ and a document set $D$, we define the average document frequency of $t$ in $D$ to be $p_t(D) = |D_t|/|D|$. Intuitively, it means that on the average any document in $D$ has probability $p_t(D)$ to contain the term $t$.

We define the text-mining function as follow:

$$f(t) = \frac{\max(p_t(A), p_t(B)) + k}{\min(p_t(A), p_t(B)) + k},$$

where a constant $k$ is added to avoid the case $f(t) = \infty$ when $p_t(A)$ or $p_t(B)$ equals 0. We set $k$ to be 0.02 in our experiments. To better understand how this function works, consider the case that $p_t(A) \geq p_t(B)$ and $k=0$. Then $f(t) = p_t(A)/p_t(B)$ and a bigger $f(t)$ has the higher ratio of $p_t(A)$ to $p_t(B)$. Thus a high-scored $f(t)$ means that the average document frequency of term $t$ in $A$ is significantly different from that in $B$.

The top 5 unigrams and top 10 bigrams obtained through $f(t)$ are given in Table 1. We remark that we studied the top 30 unigrams and bigrams, and they all showed

| $t$ | $f(t)$ | $|A_t|$ | $|B_t|$ |
|-----|--------|--------|--------|
| 1 著 | 31.0   | 0      | 24     |
| 2 知端 | 27.9   | 43     | 0      |
| 3 未知 | 24.5   | 1      | 31     |
| 4 一語 | 22.9   | 35     | 0      |
| 5 嬤嬤 | 22.3   | 34     | 0      |

Table 1. The top 5 high-scored unigrams and top 10 bigrams computed by the mining function $f(t)$.

1 http://cls.hs.yzu.edu.tw/hlm/
similar behavior.

2.3 Some findings

We now briefly discuss some of our findings. The top-scored unigram *ma* (嗎) occurs only in the form of *mama* (嬤嬤) which we shall discuss later. The unigram *li* (裡) is interchangeable with another *li* (裏), which means that this word might have been replaced during transcribing and should not be considered. However, it is interesting to remark that while *li* (裡) appears 109 times in the first 80 chapters (none in the last 40), 54 times of which are in Chapter 67 alone! This strongly suggests that the current Chapter 67 (missing in the *gengchen* edition) was later added by another person. The frequency distribution of the third unigram *ma* (嗎), a common function word, coincides with the experiments of Zhao and Chen (1975). Note that it only appeared once in the first 80 chapters. After comparing the text with some other editions, we suspect that the single paragraph containing *ma* (嗎) in the first 80 chapters was not written by Cao Xueqin.

The bigrams reveal even more insight. First consider *qizhi* (豈知, which does not have clear semantics by itself), which occurs in 24 chapters in corpus *B* but none in corpus *A*. Assuming that both *A* and *B* are written by the same author, and that the probability of this term to occur in a chapter is 24/40=0.6. Then the probability that *qizhi* is not found in text *A* is $(1-0.6)^{80} = 1.46 \times 10^{-32}$, an incredibly small number. Furthermore, the bigram *weizhi* (未知) appears in 31 chapters of the last 40, and the only chapter of the first 80 in which it appears is Chapter 64, another chapter missing in the *gengchen* edition. This provides another evident that both chapters (64 and 67) were added later by someone else. The third example, the bigram *mama* (嬤嬤, a respectful title given to an elder wet nurse) occurs in 34 out of the first 80 chapters but none in the last 40. There are many *mama’s* in DRC. They all conspicuously disappeared after Chapter 80. The 9th bigram *quxiao* (取笑, poking fun) also appeared in 30 of the first 80 chapters but totally disappeared afterwards.

2.4 The three-author question?

Recall that Yang (2003) also did not chose function words *a priori* and found strong discrepancies between Chapter 1-20, 21-80, and 81-120. Thus, if one is to conclude from their studies that the last 40 chapters were written by a different author, one may also need to declare that the first 80 chapters were also written by two different authors.

To make sure that our method does not pose similar problems, we ran the same experiment between the texts of Chapters 1-20 and Chapters 21-80. Not surprisingly,
we found some unigrams and bigrams that appear in one corpus but not in the other. A careful analysis, however, shows that they are mostly event-dependent, involving persons or places that appeared later in the story or died. Considering that there are more than 400 characters in DRC, such event-dependent differences are expected.

3. Discussions

Our studies support the thesis that the last 40 chapters of DRC were written by someone other than Cao Xueqin. It also shows that Chapters 64 and 67 may also have been written by another person. Furthermore, the text-mining method we used offers a different approach to the author attribution problem.

A common textual analysis approach is to use function words to detect discrepancies in different texts. For instance, in Chinese ma (嗎) as a function word has the equivalent me (麼). Suppose one uses ma as a proof that an article is not written by a certain person, can the verdict be overturned if one uniformly replaces all the function word occurrences of ma by me?

The text-mining approach proposed here is different. Although it is also based on differences in word style, the words are generated by the method itself. Take the term mama as an example. Mama appeared in 34 of the first 80 chapters, and was used to address quite a few minor characters in the book (last appearance in Chapter 80). However, not only was the term completely missing from the last 40 chapters, so did the concept and the characters! Such "semantic" differences seem to provide more solid evidence than purely syntactic ones.

References


Guang-Gu He (2002), From Chinese function words to the characteristics of authors – also the author attribution problem of Dream of the Red Chamber, Traditional Chinese Literature e-Journal, Hualian.


Roger Peng and Nicolas Hengartner (2001), *Quantitative Analysis of Literacy Styles*. Department of Statistics Papers, Department of Statistics, UCLA.


Gang Zhao and Zhongyi Chen (1975), 《紅樓夢研究新編》 *A New Compilation on the research of The Dream of The Red Chamber*, Linking Publishing, Taipei.